CLAIMS

| 1 | 1. A general purpose computer system having multiple nodes, comprising: |
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| 2 | at least one processor executing method acts to promote tolerance of |
| 3 | faults in the system, the method acts comprising: |
| 4 | based at least in part on the faults, determining a set of nodes; |
| 5 | and |
| 6 | using nodes in the set of nodes only as points on routing paths of |
| 7 | messages, and not using any node in the set of nodes for sending or |
| 8 | receiving messages. |
| 1 | 2. The system of Claim 1, wherein the set is a lamb set. |
| 1 | 3. The system of Claim 2, wherein the act of determining undertaken by |
| 2 | the processor includes: |
| 3 | finding small sets of partitions of candidate lamb nodes, each partition |
| 4 | including a representative node. |
| | |
| 1 | 4. The system of Claim 3, wherein the act of finding undertaken by the |
| 2 | processor includes: |

| | 3 | partitioning nodes in the system into maximal intervals of sequential |
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| | 4 | nodes, no node in an interval being a faulty node. |
| | | |
| | 1 | 5. The system of Claim 4, wherein the act of finding undertaken by the |
| | 2 | processor further includes: |
| | 3 | returning at least some intervals as at least one set of partitions. |
| | | |
| 2 | 1 | 6. The system of Claim 3, wherein the act of determining undertaken by |
| | 2 | the processor includes: |
| | 3 | determining a reachability from at least one representative node to at |
| S SHOW . | 4 | least another representative node; and |
| | 5 | using the reachability to establish a solution set, such that any node in |
| | 6 | the solution set can reach any other node in the solution set in at most k |
| | 7 | rounds. |
| | | |
| | 1 | 7. The system of Claim 6, wherein the act of determining a reachability |
| | 2 | undertaken by the processor includes: |
| | 3 | computing at least one reachability matrix, using the solution set. |
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| 1 | 8. The system of Claim 7, wherein the act of determining a reachability |
|---|---|
| 2 | undertaken by the processor further includes: |
| 3 | computing at least one intersection matrix. |
| | |
| 1 | 9. The system of Claim 8, wherein the act of determining a reachability |
| 2 | undertaken by the processor further includes: |
| 3 | returning at least one product of at least one reachability matrix and at |
| 4 | least one intersection matrix. |
| | |
| 1 | 10. The system of Claim 6, wherein k equals two. |
| | |
| 1 | 11. The system of Claim 6, wherein the act of determining undertaken by |
| 2 | the processor includes: |
| 3 | minimizing a solution set using at least one weighted graph G. |
| | |
| 1 | 12. The system of Claim 11, wherein the weighted graph is a weighted |
| 2 | bipartite graph. |
| | |
| 1 | 13. The system of Claim 11, wherein the act of minimizing undertaken by |
| 2 | the processor includes: |
| 3 | finding at least one vertex cover C of the graph G. |

| 1 | 14. The system of Claim 13, wherein the act of minimizing undertaken by |
|---|--|
| 2 | the processor further includes: |
| 3 | using selected elements of the vertex cover C, establishing the lamb set. |
| | |
| 1 | 15. The system of Claim 1, wherein membership in the set of nodes |
| 2 | depends at least partially on a number of processors in a node that are malfunctioning |
| 3 | or not functioning. |
| | |
| 1 | 16. A computer program device comprising: |
| 2 | a computer program storage device readable by a digital processing |
| 3 | apparatus; and |
| 4 | a program on the program storage device and including instructions |
| 5 | executable by the digital processing apparatus for promoting fault tolerance in a multi- |
| 6 | node system, the program comprising: |
| 7 | means for designating a lamb set of nodes in the multi-node system to |
| 8 | be used for routing messages within the system. |
| | |
| 1 | 17. The device of Claim 16, wherein the lamb set of nodes contains nodes |
| 2 | that are used only in messages routes. |

| 1 | 18. The device of Claim 16, further comprising means for finding small set |
|---|--|
| 2 | of partitions of prospective lamb nodes, each partition including a representative node. |
| 1 | 19. The device of Claim 18, wherein the means for finding includes: |
| 2 | means for partitioning nodes in the system into maximal intervals of |
| 3 | sequential nodes, no node in an interval being a faulty node. |
| 1 | 20. The device of Claim 19, wherein the means for finding includes: |
| 2 | means for returning at least some intervals as at least one set of |
| 3 | partitions. |
| 1 | 21. The device of Claim 18, wherein the means for designating includes: |
| 2 | means for determining a reachability from at least one representative |
| 3 | node to at least another representative node; and |
| 4 | means for using the reachability to establish a solution set, such that any |
| 5 | node in the solution set can reach any other node in the solution set in at most |
| 6 | k rounds. |
| 1 | 22. The device of Claim 21, wherein the means for designating includes: |
| 2 | means for computing at least one reachability matrix; |

means for computing at least one intersection matrix; and

| 4 | | means for returning at least one product of at least one reachability |
|-----|---------------------|--|
| 5 | matrix | and at least one intersection matrix. |
| 1 | 23. | The device of Claim 21, wherein k equals two. |
| 1 | 24. | The device of Claim 18, wherein the means for designating includes: |
| 2 | | means for minimizing a solution set using at least one weighted graph |
| 3 | G. | |
| 1 2 | 25. bipartite grap. | The device of Claim 24, wherein the weighted graph is a weighted |
| _ | orparente grap | |
| 1 | 26. | The device of Claim 24, wherein the means for minimizing includes: |
| 2 | | means for finding at least one vertex cover C of the graph G. |
| | | |
| 1 | 27. | The device of Claim 26, further comprising: |
| 2 . | | means for using selected elements of the vertex cover C to establish the |
| 3 | lamb s | set. |

| 1 | 28. The device of Claim 16, wherein membership in the lamb set of nodes |
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| 2 | depends at least partially on a number of processors in a node that are malfunctioning |
| 3 | or not functioning. |
| | |
| 1 | 29. A method for promoting fault tolerance in a multi-node system, |
| 2 | comprising the acts of: |
| 3 | for each of k rounds, finding multiple partitions of nodes, each partition |
| 4 | having a representative node; |
| 5 | for each representative node, determining whether the node can reach at |
| 6 | least one predetermined other representative node within a predetermined |
| 7 | criteria; |
| 8 | minimizing the number of nodes and/or partitions using a weighted |
| 9 | graph to establish a routing set of nodes; and |
| 10 | returning the routing set of nodes for use thereof in routing messages |
| 11 | through the system in the presence of one or more node and/or link faults. |
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| 1 | 30. The method of Claim 29, wherein the number of rounds is at most two. |
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| 1 | 31. The method of Claim 29, wherein the number of rounds is two and only |
| | |

two.

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| 1 | 32. | The method of Claim 29, wherein the weighted graph accounts for at |
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| 2 | least one nod | le weight, the node weight being based at least on a number of operational |
| 3 | processors in | the node. |
| | | |
| 1 | 33. | The method of Claim 29, wherein the routing set of nodes is a lamb set |
| 2 | containing no | odes that are used only for routing messages. |
| | | |
| 1 | 34. | The method of Claim 29, further comprising finding small sets of |
| 2 | partitions of | prospective lamb nodes, each partition including a representative node. |
| | | |
| 1 | 35. | The method of Claim 34, comprising partitioning nodes in the system |
| 2 | into maximal | intervals of sequential nodes, no node in an interval being a faulty node. |
| | | |
| 1 | 36. | The method of Claim 35, comprising returning at least some intervals as |
| 2 | at least one s | et of partitions. |
| | | |
| 1 | 37. | The method of Claim 29, wherein the act of determining whether the |
| 2 | node can read | ch at least one predetermined other node comprises: |
| 3 | | determining a reachability from at least one representative node to at |

least another representative node; and

| 5 | using the reachability to establish the routing set, such that any node in |
|---|--|
| 6 | the routing set can reach any other node in the routing set in at most k rounds. |
| | |
| 1 | 38. The method of Claim 37, wherein the act of determining whether the |
| 2 | node can reach at least one predetermined other node comprises: |
| 3 | computing at least one reachability matrix; |
| 4 | computing at least one intersection matrix; and |
| 5 | returning at least one product of at least one reachability matrix and at |
| 6 | least one intersection matrix. |
| | |
| 1 | 39. The method of Claim 29, wherein the act of minimizing includes: |
| 2 | finding at least one vertex cover of the weighted graph; and |
| 3 | using selected elements of the vertex cover to establish the routing set. |
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| 1 | 40. The method of Claim 29, wherein the weighted graph is a weighted |

bipartite graph.